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Inverse Trigonometric Functions: Properties of Inverse Part 1 (For CBSE, ICSE, IAS, NET, NRA 2022)

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What is Inverse Trigonometric Function?

Considering the Domain and Range of the Inverse Functions, Following Formulas Are Important to Be Noted:

$$\sin (\sin ^{-1} x)=x, \text { if }-1 \leq x \leq 1$$

$$\cos \left(\cos ^{-1} x\right)=x, \text { if }-1 \leq x \leq 1$$

$$\tan \left(\tan ^{-1} x\right)=x, \text { if }-\infty \leq x \leq \infty$$

$$\cos \left(\cos ^{-1} x\right)=x, \text { if }-\infty \leq x \leq \infty$$

$$\cot \left(\cot ^{-1} x\right)=x, \text { if }-\infty \leq x \leq \infty$$

$$\sec \left(\sec ^{-1} x\right)=x, \text { if }-\infty \leq x \leq-1 \text { or } 1 \leq x \leq \infty$$

$$\operatorname{cosec}\left(\operatorname{cosec}^{-1} x\right)=x, \text { if }-\infty \leq x \leq-1 \text { or } 1 \leq x \leq \infty$$

- The inverse trigonometric functions are an important aspect of trigonometric functions, included in the syllabus for class 12 students.
- In mathematics, the inverse trigonometric functions are the inverse functions of the trigonometric functions.
- Inverses of trigonometric functions exist solely due to the restrictions existing on the domains and their respective ranges.
- Being able to solve inverse trigonometric function problems starts by understanding the trigonometric ratios first.
- Specifically, they are the inverses of the sine, cosine, tangent, cotangent, secant, and cosecant functions, and are used to obtain an angle from any of the angle's trigonometric ratios
- The behavior of these trigonometric functions is usually represented in the form of graphical methods.
- They play an essential role in calculus as they help to define different integrals.

- Major applications of inverse trigonometric functions in everyday life are in the fields of science and engineering.

Properties of Inverse Trigonometric Functions

- The properties of Inverse Trigonometric Functions help to prove a distinct relationship between the different trigonometric entities such as $\sin x$, $\cos x$, $\tan x$, $\csc x$, $\sec x$, and $\cot x$.
- There are a few inverse trigonometric functions properties which are crucial to not only solve problems but also to have a deeper understanding of this concept.
- The domain of a function is defined as the set of every possible independent variable where the function exists. Inverse Trigonometric Functions are defined in a certain interval.
- The results obtained with the help of these properties are valid within the principal branches of the inverse trigonometric functions.
- To recall, inverse trigonometric functions are also called “Arc Functions.” For a given value of a trigonometric function; they produce the length of arc needed to obtain that value.
- These properties are valid for some values of x , where these inverse trigonometric functions are defined with.
- The range of an inverse function is defined as the range of values of the inverse function that can attain with the defined domain of the function.

Property Set 1

$$\sin^{-1}(x) = \csc^{-1}\left(\frac{1}{x}\right), x \in [-1, 1] - \{0\}$$

$$\cos^{-1}(x) = \sec^{-1}\left(\frac{1}{x}\right), x \in [-1, 1] - \{0\}$$

$$\tan^{-1}(x) = \cot^{-1}\left(\frac{1}{x}\right), \text{if } x > 0 \text{ (or) } \cot^{-1}\left(\frac{1}{x}\right) - \pi, \text{if } x < 0$$

$$\cot^{-1}(x) = \tan^{-1}\left(\frac{1}{x}\right), \text{if } x > 0 \text{ (or) } \tan^{-1}\left(\frac{1}{x}\right) + \pi, \text{if } x < 0$$

Property Set 2

$$\sin^{-1}(-x) = -\sin^{-1}(x)$$

$$\tan^{-1}(-x) = -\tan^{-1}(x)$$

$$\cos^{-1}(-x) = \pi - \cos^{-1}(x)$$

$$\sec^{-1}(-x) = \pi - \sec^{-1}(x)$$

$$\cot^{-1}(-x) = \pi - \cot^{-1}(x)$$

Derivatives of Inverse Trigonometric Functions

$$\frac{d}{dx}(\sin^{-1} x) = \frac{1}{\sqrt{1-x^2}}, x \neq \pm 1$$

$$\frac{d}{dx}(\cos^{-1} x) = \frac{-1}{\sqrt{1-x^2}}, x \neq \pm 1$$

$$\frac{d}{dx}(\tan^{-1} x) = \frac{1}{1+x^2}$$

$$\frac{d}{dx}(\cot^{-1} x) = \frac{-1}{1+x^2}$$

$$\frac{d}{dx}(\sec^{-1} x) = \frac{1}{|x| \sqrt{x^2-1}}, x \neq \pm 1, 0$$

$$\frac{d}{dx}(\csc^{-1} x) = \frac{-1}{|x| \sqrt{x^2-1}}, x \neq \pm 1, 0$$

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